## The Function Eval

Evaluation is an implicit action of the ALU. By claiming evaluation is automatic, we are committed to wiring the ALU in a specific way. However handling memory can be made flexible by *defining* **Eval** *in the programming language itself*. This process is called *meta-circular evaluation*, cause it uses a language itself to define how that language should behave. All we have to do is to define the evaluation function by telling the system what to do when an expression is typed in. The function **Eval** takes two arguments, the expression to be evaluated and the *binding environment*, that is, an address of the memory array which contains all of the primitive functions and atoms (and any other symbols which we may have added) in the language. The binding environment contains the definitions of all user defined functions, and the values of each of the variables (function arguments).

Since the binding environment does not change in this example, (i.e. we have not designed the language to establish separate environments for each function call), we will treat the token **Eval** to mean "Eval-in-environment". (Some of the syntax has been changed to make **Eval** more readable.)

The definition of **Eval** which follows recognizes only seven reserved words as primitive functions. In addition, **Eval** uses three built-in tests to determine the types of objects.

First	Rest	Cons	
lfThenElse	Equal	Quote	Let
ls-empty	lsa-atom	lsa-expression	

[Notes and supporting functions are on this page to save space. Eval itself is on the next page.]

*Notes,* \* process Atom in First: This defines a syntax for parsing. Every expression begins with an atom or is an atom. If an expression begins with an atom, the processor assumes that that atom is an operator, and thus a processing instruction. The operator **Quote** is the no-op.

*Notes,* \*\* Cons Eval of Rest: This is again a syntax constraint. Once we have removed the beginning operator of an expression, what follows is either an atom, or another expression which itself begins with an atom operator.

```
EvalLogic exp =def=
                                                               ; if First is TRUE
      If Equal (Eval (First exp)) (Quote True)
                                                               ;Eval second argument
       Then
         Eval (Rest exp)
                                                               ;Eval third argument
       Else
         Eval (Rest (Rest exp)))
EvalExp exp
               =def=
      If Is-empty exp
                                                               ; if at the end
                                                               ; return ground
       Then
         nil
                                                               ;Eval the parts
       Else
                                                               ; and put them together
        Cons (Eval (First exp)) (Eval (Rest exp))
```

```
Eval exp =def=
If Isa-atom exp
 Then
                                                                ; process atom
   If Is-empty (First exp)
                                                                return the SYMBOL
    Then
      Rest exp
                                                                ; or its VALUE
    Else
      First exp
 Else
                                                                ; process expression
   If Isa-atom (First exp)
                                                                ; process Atom in First*
    Then
                                                                ; naming the atom
      Let token (First exp)
         If Equal token (Quote Quote)
                                                                ; return what follows
         Then
            Rest exp
                                                                   ; other operators
         Else
            If Equal token (Quote IfThenElse)
                                                                ; process logic operator
             Then
               EvalLogic (Rest exp)
                                                                   ; other operators
             Else
               If Equal token (Quote First)
                                                                : First of Eval of Rest
                Then
                  First (Eval (Rest exp))
                                                                  ; other operators
                Else
                  If Equal token (Quote Rest)
                                                                ;Rest of Eval of Rest
                    Then
                      Rest (Eval (Rest exp))
                                                                  ; other operators
                    Else
                      If Equal token (Quote Isa-atom)
                                                                ; Isa-atom Eval of Rest
                       Then
                         Isa-atom (Eval (Rest exp))
                                                                   ; other operators
                       Else
                         If Isa-expression token
                                                                ; process expression
                          Then
                            EvalExp (Rest exp)
                                                                  ; other operators
                          Else
                            If Equal token (Quote Cons)
                                                                ;Cons Eval of Rest**
                              Then
                                Cons (Eval (Rest exp))
                                       (Eval (Rest (Rest exp)))
                                                                   ; other operators
                              Else
                                If Equal token (Quote Equal)
                                                                ;Equal Eval of args
                                 Then
                                   Equal (Eval (Rest exp))
                                           (Eval (Rest (Rest exp)))
                                                                ; replace the token
                                 Else
                                                                ; with its value
                                   Eval
                                       Cons (First token) (Rest exp)
    Else ERROR))
```

2