

(VERY) BIG NUMBERS

The Thirsty Archeologist Exercise

An archeologist was digging in a Paleozoic mudflat when she came across an imprint of a raindrop that fell 300 million years ago. She took a drink from her canteen. How many molecules of the original raindrop did she drink?

Some information:

water on Earth:	326 million cubic miles
	1.36×10^9 cubic kilometers
	1.36×10^{24} cc

98 % of this water is in the Oceans
 .001 % is in the atmosphere

1 cc water = 1 gram
 1 drink = 100 grams
 1 raindrop = 1×10^{-1} grams

molecules in 1 gram of water:	$6/18 \times 10^{23}$
	3×10^{22}

Avogadro's number: 6×10^{23}

molecules of water on Earth = 4×10^{46}
 molecules of water in drink = 3×10^{24}
 molecules of water in drop = 3×10^{21}

size of random sample with one molecule from drop
 = molecules on Earth / molecules in drop
 = 1×10^{25} molecules

So 1 molecule every 3 drinks.

Population of People on Earth:	6.5 billion
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National debt of the USA:	$\$9.5 \times 10^{12}$
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Number of bytes sent over the Internet (per second):	?
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Stars in our galaxy:	300 billion (3 x 10 ¹¹)
Galaxies in the Universe:	>100 billion
Weight of average star:	2 x 10 ³³ grams
Hydrogen molecules per average star:	1 x 10 ⁵⁷
Hydrogen molecules per average galaxy:	3 x 10 ⁶⁸
Visible matter in the Universe:	
All matter in the Universe:	20 x visible matter
Atoms in the Universe:	4-8 x 10 ⁷⁹ atoms of H
Age of the Universe:	14 billion years
Diameter of the Universe:	156 billion light years (Baez error) 92 billion light-years (Wiki)
Volume of the Universe:	3 x 10 ⁸⁰ cubic meters 3 x 10 ⁸⁶ cc
Diameter of H atom proton:	10 ⁻¹⁵ meters 10 ⁻¹³ centimeters
Protons packed in a cc:	10 ³⁹
Protons to fill entire Universe:	3 x 10 ¹²⁵
Ways to arrange protons packed into the Universe:	(3 x 10 ¹²⁵)!

Sterling approximation: $N! = (N/e)^N \sqrt{2\pi N}$

$$N/e = 10^{125}$$

$$2\pi N = 2 \times 10^{126}$$

$$\sqrt{2\pi N} = 10^{63}$$

$$N \sqrt{2\pi N} = 3 \times 10^{188}$$

$$(10^{125})^{(3 \times 10^{188})} = 10^{(3 \times 10^{(125 \times 188)})}$$

$$10^{(3 \times 10^{23500})}$$

(10²³⁵⁰⁰) is 10 followed by 23500 zeros

10^(10²³⁵⁰⁰) is 10 followed by that many zeros.